

$$|x| = \begin{cases} x, & \text{for } x \geq 0 \\ -x, & \text{for } x < 0 \end{cases} \quad (1)$$

$$(2)$$

Another example is calculating the square root of  $c + id$ . First compute

$$w \equiv \begin{cases} 0 & c = d = 0 & (3a) \\ \sqrt{|c|} \sqrt{\frac{1 + \sqrt{1 + (d/c)^2}}{2}} & |c| \geq |d| & (3b) \\ \sqrt{|d|} \sqrt{\frac{|c/d| + \sqrt{1 + (c/d)^2}}{2}} & |c| < |d| & (3c) \end{cases}$$

Then, using  $w$  from eq. (3), the square root is

$$\sqrt{c + id} = \begin{cases} 0 & w = 0 \text{ (case 3a)} & (4a) \\ w + i\frac{d}{2w} & w \neq 0, c \geq 0 & (4b) \\ \frac{|d|}{2w} + iw & w \neq 0, c < 0, d \geq 0 & (4c) \\ \frac{|d|}{2w} - iw & w \neq 0, c < 0, d < 0 & (4d) \end{cases}$$